



## CHAPTER 1

### **Introduction**

Let  $p$  be a fixed prime number. Let  $\mathbb{Q}_p$  denote the field of  $p$ -adic rational numbers and fix an algebraic closure  $\mathbb{Q}_p^{alg}$ . For  $K$  a finite extension of  $\mathbb{Q}_p$  (called  *$p$ -adic field*) we know that there exists only finite number of extensions of given degree (See [4, p.54], Proposition 14). Krasner has told us this fact. In chapter 2, we give some notations and preliminary results about  $\mathbb{Q}_p$  and introduce unramified and totally ramified extensions of  $\mathbb{Q}_p$ . In chapter 3, we find polynomials generating all totally ramified extensions and calculate the number. In chapter 4 and 5, we discuss extensions of  $\mathbb{Q}_p$  of degree 2 and 3, respectively.

